

# Efficiency Maximization of Wireless Power Transfer Based on Simultaneous Estimation of Generalized Two Parameters

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**Abstract**—A dynamic wireless power transfer (WPT) system for electric vehicles has to simplify its road-side facilities, which are installed over long distances. Although previous research has proposed secondary-side efficiency control, design constraints of the WPT system have to be imposed to obtain the reference value of the control. In this paper, an efficiency maximization method based on simultaneous estimation of the generalized two parameters, which determine the reference value of the control, is proposed. Since the generalized two parameters are estimated using secondary-side information, the design constraints of the WPT system can be eliminated. Simulations and experiments demonstrated that the estimation strategy achieved sufficient accuracy for maximum efficiency control and the proposed method drastically improved the transmitting efficiency.

**Keywords**—Wireless power transfer, Magnetic resonance coupling, Parameter estimation, Efficiency maximization

## I. INTRODUCTION

Wireless power transfer (WPT) has gathered much attention to improve convenience and reliability of transportation applications [1]–[3]. Additionally, dynamic charging of electric vehicles (EVs) is expected to expand the limited driving distance due to the energy storage system of EVs [4], [5]. In order to implement a dynamic WPT system for EVs, it is necessary to achieve a high-power and high-efficiency transmission without dependence on the vehicle motion.

WPT via magnetic resonance coupling [6] has suitable characteristics for EV charging [2]. However, its transmitting efficiency is determined not only by magnetic coupling between a transmitter and a receiver but also by a load condition, which depends on the vehicle motion in dynamic charging. As a result, it is important to apply a control strategy for maximizing the transmitting efficiency. This paper focuses on secondary-side control to simplify the road-side facilities, which are installed over long distances in the dynamic WPT system for EVs. Although previous research has proposed an efficiency maximization method on the secondary side [7], design constraints of the WPT system has to be imposed to obtain the reference value of secondary-side efficiency control.

In this paper, an efficiency maximization method based on simultaneous estimation of the generalized two parameters, which determine the reference value of the control, is proposed. The estimation strategy is described using secondary-side information and the design constraints can be eliminated

by the proposed method. The effectiveness of the proposed method is demonstrated by simulations and experiments.

## II. WIRELESS POWER TRANSFER SYSTEM

### A. System configuration

Fig. 1 shows the circuit diagram of the WPT system. The power supply consists of the DC voltage source and the full-bridge inverter. The transmitter and receiver are designed to employ a series-series (SS) compensated circuit topology of WPT via magnetic resonance coupling. The power source angular frequency  $\omega_0$  and the resonance angular frequency of the transmitter and receiver are given as follows:

$$\omega_0 = \frac{1}{\sqrt{L_1 C_1}} = \frac{1}{\sqrt{L_2 C_2}}. \quad (1)$$

Half Active Rectifier (HAR) is used as an AC-DC converter and composed of the upper arm diodes and the lower arm MOSFETs. The DC link voltage is controlled by the HAR to maximize the transmitting efficiency. The load is assumed to be a battery charging system, a motor drive system, and so on.

In order to verify the effectiveness of the proposed control strategy, the experimental equipment was implemented. The transmitter and receiver coils are shown in Fig. 2(a) and their specifications are indicated in TABLE I. The power converters, which are shown in Fig. 2(b), include the primary-side inverter and the HAR. They were controlled by a DSP (PE-PRO/F28335A, Myway) without signal communication between the primary side and the secondary side.

### B. Operation modes of HAR

HAR controls the DC link voltage  $V_{dc}$  using two different operation modes, which are shown in Fig. 3.

1) *Rectification mode*: When the lower arm MOSFETs are turned off, HAR is operated as the diode rectifier circuit. Then, the transmitting power  $P$  flows into the DC link capacitor and increases  $V_{dc}$  if  $P$  is larger than the load power  $P_L$ .

2) *Short mode*: HAR short-circuits the receiver by turning on the lower arm MOSFETs. During the short mode,  $V_{dc}$  is decreased because  $P$  is cut-off and  $P_L$  is supplied from the DC link capacitor.

By switching the operation modes according to  $V_{dc}$ , HAR can control  $V_{dc}$  within the desirable range [3].

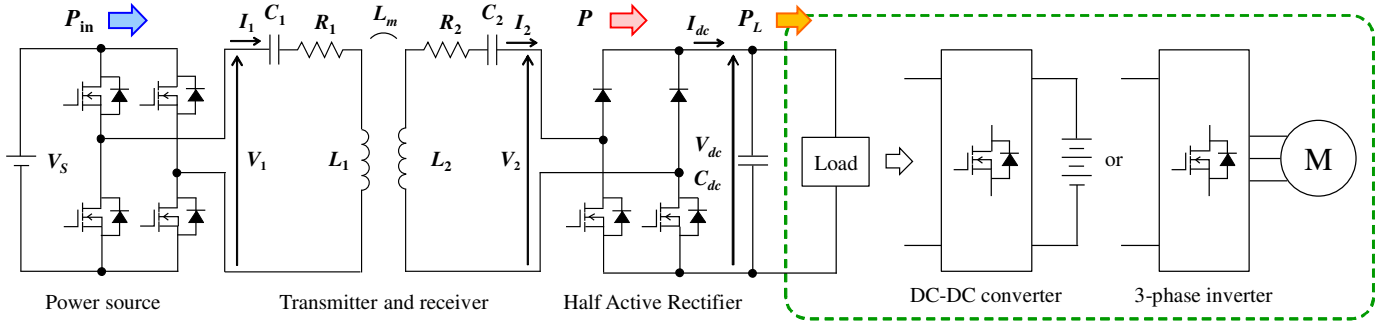
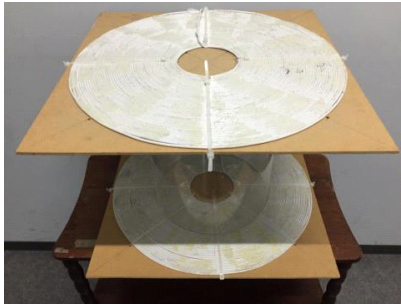
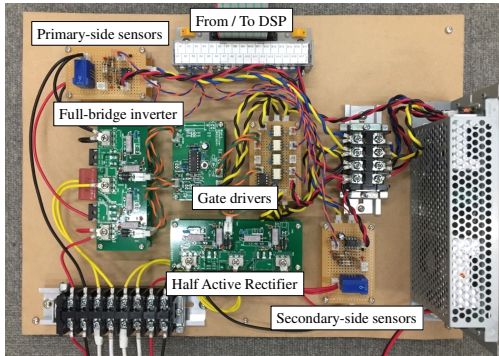


Fig. 1. Circuit diagram of the wireless power transfer system using Half Active Rectifier.



(a) Transmitter and receiver coils.



(b) Power converters.

Fig. 2. Experimental equipment.

### C. Maximum efficiency control on the secondary side

Since the transmitting efficiency is determined not only by coupling between the transmitter and receiver but also by the load condition, the reference value of  $V_{dc}$  should be given properly. Although it has already been indicated using three parameters, which are unmeasurable on the secondary side [7], a simultaneous estimation method of these three parameters using secondary-side information remains unrealized. In order to eliminate the need for signal communication between the primary side and the secondary side, some parameters have to be fixed and given by design constraints of the WPT system.

In this paper, the reference value of maximum efficiency control on the secondary side is derived using the generalized two parameters, which are estimated based on secondary-side information. Additionally, a simultaneous estimation method of the generalized two parameters is described in chapter IV.

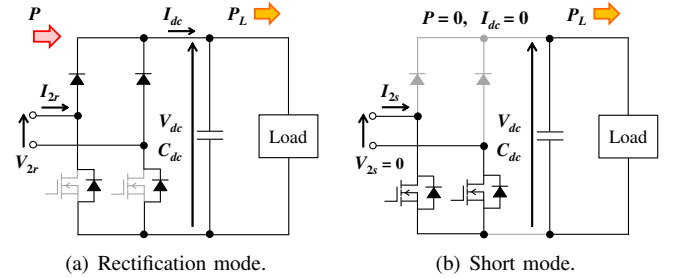


Fig. 3. Operation modes of Half Active Rectifier.

TABLE I. SPECIFICATIONS OF TRANSMITTER AND RECEIVER.

	Transmitter	Receiver
Resistance $R_1, R_2$	1.19 $\Omega$	1.23 $\Omega$
Inductance $L_1, L_2$	617 $\mu\text{H}$	617 $\mu\text{H}$
Capacitance $C_1, C_2$	4000 pF	4000 pF
Resonance frequency $f_1, f_2$	101.3 kHz	101.3 kHz
Mutual inductance $L_m$	37.3 $\mu\text{H}$ (Gap: 300 mm)	77.8 $\mu\text{H}$ (Gap: 200 mm)
Coupling coefficient $k$	0.060 (Gap: 300 mm)	0.126 (Gap: 200 mm)
Outer diameter	440 mm	
Number of turns	50 turns	

## III. CIRCUIT ANALYSIS

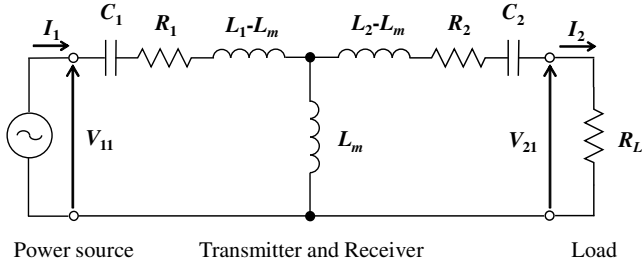
In this chapter, the circuit analysis of the WPT system is indicated to derive the reference value of maximum efficiency control on the secondary side. Then, a resistive load and a constant voltage load are addressed.

### A. Resistive load condition

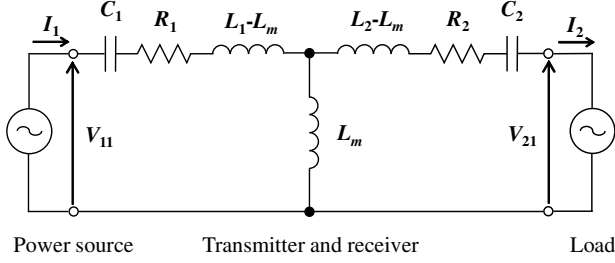
Fig. 4(a) shows the equivalent circuit of WPT via magnetic resonance coupling using the resistive load [8]. In this study, iron loss is assumed to be negligible small. When the primary-side inverter generates a square voltage wave, the RMS value of the fundamental primary voltage  $V_{11}$  is expressed as follows:

$$V_{11} = \frac{2\sqrt{2}}{\pi} V_1 = \frac{2\sqrt{2}}{\pi} V_S. \quad (2)$$

Then, the voltage ratio  $A_V$  and the current ratio  $A_I$  between the primary side and the secondary side are given



(a) Resistive load.



(b) Constant voltage load.

Fig. 4. Equivalent circuit of wireless power transfer via magnetic resonance coupling.

as follows:

$$A_V = \frac{V_{21}}{V_{11}} = \frac{\omega_0 L_m R_L}{R_1(R_2 + R_L) + (\omega_0 L_m)^2} \quad (3)$$

$$A_I = \frac{I_2}{I_1} = \frac{\omega_0 L_m}{R_2 + R_L} \quad (4)$$

where  $V_{21}, I_1, I_2$  are the RMS values of the fundamental secondary voltage, the primary current, and the secondary current, respectively.

From eq. (3) and eq. (4), the transmitting efficiency  $\eta$  and the charging power  $P$  are described as follows:

$$\eta = \frac{(\omega_0 L_m)^2 R_L}{(R_2 + R_L)\{R_1(R_2 + R_L) + (\omega_0 L_m)^2\}} \quad (5)$$

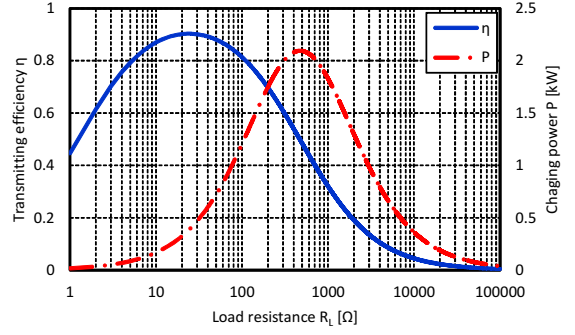
$$P = \frac{A_V^2}{R_L} V_{11}^2 = \frac{(\omega_0 L_m)^2 R_L}{\{R_1(R_2 + R_L) + (\omega_0 L_m)^2\}^2} V_{11}^2. \quad (6)$$

When  $V_{11} = 100$  V and  $L_m = 77.8$   $\mu$ H, Fig. 5(a) shows  $R_L$  versus  $\eta$  and  $P$ . Then, the load resistance  $R_{L\eta\max}$ , which maximizes  $\eta$ , is given as follows [9]:

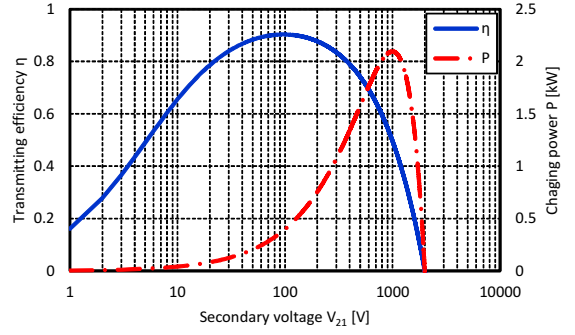
$$R_{L\eta\max} = \sqrt{R_2 \left\{ \frac{(\omega_0 L_m)^2}{R_1} + R_2 \right\}}. \quad (7)$$

### B. Constant voltage load condition

Since the DC link voltage  $V_{dc}$  is controlled on the secondary side, the actual load has to be assumed not as the resistive load but as the constant voltage load. The equivalent circuit of WPT via magnetic resonance coupling using the constant voltage load is shown in Fig. 4(b). Then,  $V_{21}$  has to be given both during the rectification mode and during the short mode of HAR.



(a) Resistive load.



(b) Constant voltage load.

Fig. 5. Transmitting efficiency  $\eta$  and charging power  $P$ .

Because the rectification mode of HAR is worked as the diode rectifier, the secondary voltage is assumed to be a square wave with the same amplitude as the DC link voltage and the same frequency as the primary voltage if the voltage variation in  $V_{dc}$  is negligible small [10]. On the other hand, the secondary voltage during the short mode of HAR equals to 0 because the receiver is shorted.

When  $V_{21r}, V_{21s}$  are defined as the fundamental secondary voltage during the rectification mode and during the short mode, they are calculated as follows:

$$V_{21r} = \frac{2\sqrt{2}}{\pi} V_{2r} = \frac{2\sqrt{2}}{\pi} (V_{dc} + 2V_f) \quad (8)$$

$$V_{21s} = \frac{2\sqrt{2}}{\pi} V_{2s} = 0 \quad (9)$$

where  $V_f$  is the forward voltage of the diodes.

Additionally, the phase difference between the primary voltage and the secondary voltage is assumed to be 90 degrees [10]. From the circuit equation, the secondary current  $I_2$  is calculated as follows:

$$I_2 = \frac{\omega_0 L_m V_{11} - R_1 V_{21}}{R_1 R_2 + (\omega_0 L_m)^2}. \quad (10)$$

Then, the equivalent resistance of the constant voltage load  $R_L$  is obtained as follows:

$$R_L = \frac{V_{21}}{I_2} = \frac{\{R_1 R_2 + (\omega_0 L_m)^2\} V_{21}}{\omega_0 L_m V_{11} - R_1 V_{21}}. \quad (11)$$

Consequently, the constant voltage load can be treated equally with the resistive load as shown in Fig. 4(a).

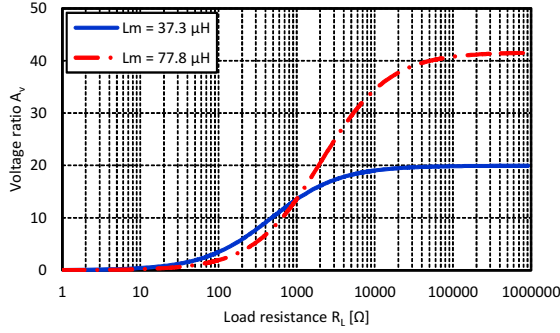


Fig. 6. Load resistance  $R_L$  vs. voltage ratio  $A_V$ .

When  $V_{11} = 100$  V and  $L_m = 77.8$   $\mu$ H, Fig. 5(b) shows  $V_{21}$  versus  $\eta$  and  $P$ . From eq. (3) and eq. (7), the fundamental secondary voltage  $V_{21\eta_{\max}}$ , which maximizes  $\eta$ , is expressed as follows [7]:

$$V_{21\eta_{\max}} = \sqrt{\frac{R_2}{R_1}} \frac{\omega_0 L_m}{\sqrt{R_1 R_2 + (\omega_0 L_m)^2} + \sqrt{R_1 R_2}} V_{11}. \quad (12)$$

However, eq. (12) includes the fundamental primary voltage  $V_{11}$ , the primary coil resistance  $R_1$ , and the mutual inductance between the transmitter and the receiver  $L_m$ , which are unmeasurable on the secondary side. Although previous research has proposed a simultaneous estimation method of  $V_{11}$  and  $L_m$  [11],  $R_1$  has to be fixed and given by the design constraints of the WPT system.

### C. Generalized two parameters

This paper derives  $V_{21\eta_{\max}}$  using the generalized two parameters  $x_1, x_2$ , which are defined as follows:

$$x_1 = k^2 Q_1 Q_2 = \frac{(\omega_0 L_m)^2}{R_1 R_2} \quad (13)$$

$$x_2 = V_{21\max} = \frac{\omega_0 L_m V_{11}}{R_1} \quad (14)$$

where  $x_1, x_2$  are given to include  $V_{11}$ ,  $R_1$ , and  $L_m$ . Then,  $x_1$  implies maximum efficiency of the WPT system [2], [12] and  $x_2$  is the fundamental value of the maximum available secondary voltage  $V_{21\max}$ . Fig. 5(b) shows that  $V_{21\max}$  exists when  $P$  equals to 0 excluding  $V_{21} \neq 0$ . Then, the equivalent resistance  $R_L$ , which is given by eq. (11), becomes  $\infty$ . It is confirmed that Fig. 6 shows the voltage ratio  $A_V$  becomes saturated according to the increase in  $R_L$ . Its maximum value  $A_{V_{\text{sat}}}$  is described as follows [9]:

$$A_{V_{\text{sat}}} = \frac{V_{21\max}}{V_{11}} = \frac{\omega_0 L_m}{R_1}. \quad (15)$$

From eq. (12), eq. (13), and eq. (14),  $V_{21\eta_{\max}}$  can be derived as follows:

$$V_{21\eta_{\max}} = \frac{V_{21\max}}{1 + \sqrt{1 + k^2 Q_1 Q_2}} = \frac{x_2}{1 + \sqrt{1 + x_1}}. \quad (16)$$

Therefore, the reference value of maximum efficiency control can be calculated based on simultaneous estimation of  $x_1$  and  $x_2$  using secondary-side information without design constraints of the WPT system.

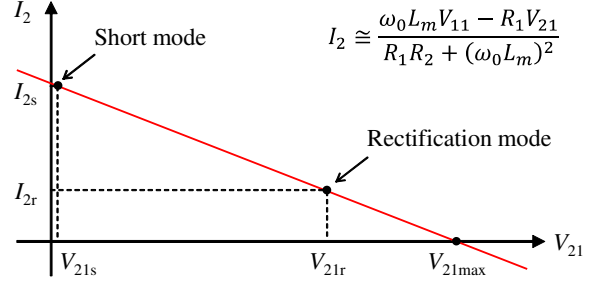


Fig. 7. Secondary current  $I_2$  in each modes of HAR.

## IV. SIMULTANEOUS ESTIMATION OF GENERALIZED TWO PARAMETERS

This chapter indicates the simultaneous estimation method of  $x_1$  and  $x_2$  using secondary-side information. The estimation equation is derived based on the theoretical equation of the secondary current  $I_2$ . Eq. (10) is transformed as follows:

$$V_{21} + R_2 I_2 + k^2 Q_1 Q_2 R_2 I_2 = V_{21\max}. \quad (17)$$

Then, the estimation equation is obtained as follows:

$$(-R_2 I_2) x_1 + x_2 = V_{21} + R_2 I_2 \quad (18)$$

Fig. 7 shows the fundamental secondary voltage  $V_{21}$  versus the secondary current  $I_2$  and the measurement points during the rectification mode and during the short mode. Since HAR utilize the two operation modes for secondary-side control,  $V_{21}$  and  $I_2$  can be measured in each modes. Because  $V_{21r}, V_{21s}$  are given by eq. (8) and eq. (9),  $I_{2r}, I_{2s}$  are theoretically calculated by eq. (10). When the unknown parameter  $x$  is defined as follows:

$$x = [x_1 \quad x_2]^T = [k^2 Q_1 Q_2 \quad V_{21\max}]^T \quad (19)$$

the estimated parameter  $\hat{x}$  is obtained as follows:

$$\hat{x} = [\hat{x}_1 \quad \hat{x}_2]^T = \mathbf{A}^{-1} \mathbf{b} \quad (20)$$

$$\mathbf{A} := \begin{bmatrix} -R_2 I_{2r} & 1 \\ -R_2 I_{2s} & 1 \end{bmatrix}, \quad \mathbf{b} := \begin{bmatrix} V_{21r} + R_2 I_{2r} \\ V_{21s} + R_2 I_{2s} \end{bmatrix}.$$

Then,  $x$  is estimated based on secondary-side information because  $V_{21r}, I_{2r}, V_{21s}$ , and  $I_{2s}$  are the measured values during the rectification mode and during the short mode. Additionally, the secondary coil resistance  $R_2$  is given on the secondary side.

## V. SIMULATION AND EXPERIMENT

### A. Experimental condition

The circuit configuration of the experimental setup is illustrated in Fig. 1. The source voltage  $V_S$  was tuned to 10 V or 20 V and the transmitting distance was set to 200 mm or 300 mm. The DC link voltage  $V_{dc}$  was regulated by an electronic load from 2.5 V to 50 V.  $I_2$  was measured during each modes of HAR and used for simultaneous estimation of the generalized two parameters  $x_1, x_2$ . The reference voltage of maximum efficiency control was calculated based on the estimated values  $\hat{x}_1, \hat{x}_2$  and efficiency improvement with maximum efficiency control using the estimated reference voltage was verified.

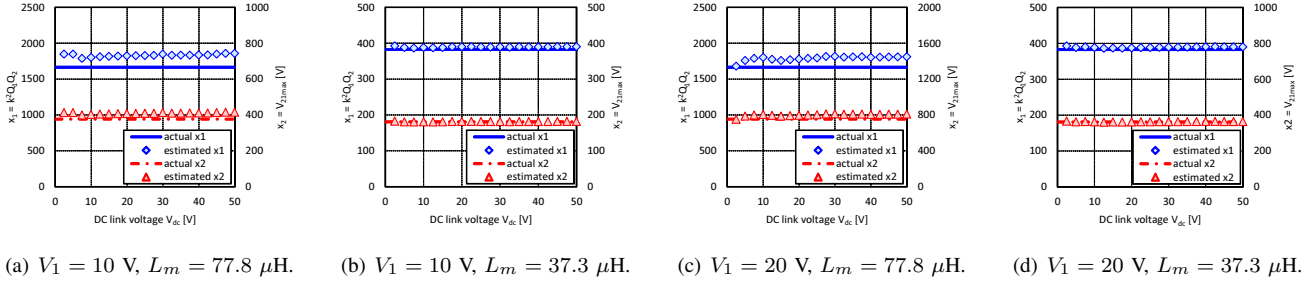


Fig. 8. Simulation results of  $x_1$  and  $x_2$  estimation.

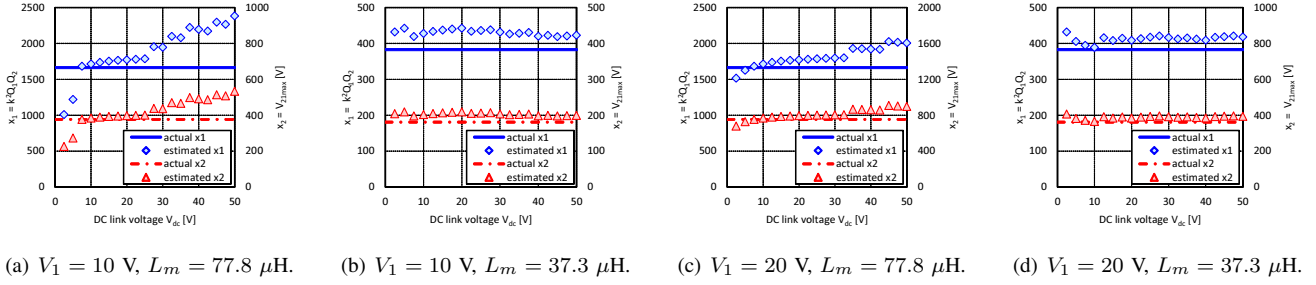


Fig. 9. Experimental results of  $x_1$  and  $x_2$  estimation.

### B. Simultaneous estimation of generalized parameters

The simulation results of  $x_1$  and  $x_2$  estimation are shown in Fig. 8. The actual values of  $x_1$  and  $x_2$  are represented by the lines and the estimation results  $\hat{x}_1, \hat{x}_2$  are indicated by the plots. From Fig. 8(a) and Fig. 8(c), which are the large  $L_m$  condition, it is confirmed that  $\hat{x}_2$  is adequately estimated but  $\hat{x}_1$  is slightly larger than  $x_1$ . This is because the difference of  $I_2$  between each operation modes of HAR is quite small. As a result, measurement capability affects the estimation accuracy. In this simulation, the measured values were rounded to 3 significant digits.

Fig. 9 shows the experimental results of  $x_1$  and  $x_2$  estimation. Although the estimation accuracy is reduced compared to the simulation results, it is important not to make a precise estimate of  $x_1$  and  $x_2$  but to obtain the reference value of the control and to maximize the transmitting efficiency. Therefore, the reference voltage calculation and efficiency maximization based on the estimation results  $\hat{x}_1, \hat{x}_2$  were demonstrated.

### C. Reference voltage calculation and efficiency maximization

Fig. 10 and Fig. 11 show the calculation results of the reference voltage based on  $\hat{x}_1, \hat{x}_2$ , which are described in Fig. 8 and Fig. 9. The calculated reference voltages are well accorded with their actual values except for Fig. 11(a). As a result, it is difficult to obtain the precise value of the reference voltage at the low power and high coupling condition.

Finally, efficiency maximization using the calculated reference voltage was verified and its results are shown in Fig. 12 and Fig. 13. If the DC link voltage is away from the optimum voltage, which maximize the transmitting efficiency  $\eta$ , before the control,  $\eta$  is drastically increased. Since efficiency degradation due to the estimation error is not confirmed, the estimation accuracy of  $x_1$  and  $x_2$  is sufficient and the proposed method is feasible for maximum efficiency control.

## VI. CONCLUSION

This paper proposed an efficiency maximization method of WPT based on simultaneous estimation of the generalized two parameters, which determine a reference value of maximum efficiency control on the secondary side. The proposed method can eliminate design constraints of the WPT system for the control because the generalized two parameters and the reference value were estimated only using secondary-side information. Simulations and experiments demonstrated that estimation accuracy of the proposed method was sufficient for the control and the transmitting efficiency was much improved by the proposed method. Future works are to implement a real-time estimation and control strategy and to apply the proposed method to EV applications.

### ACKNOWLEDGMENTS

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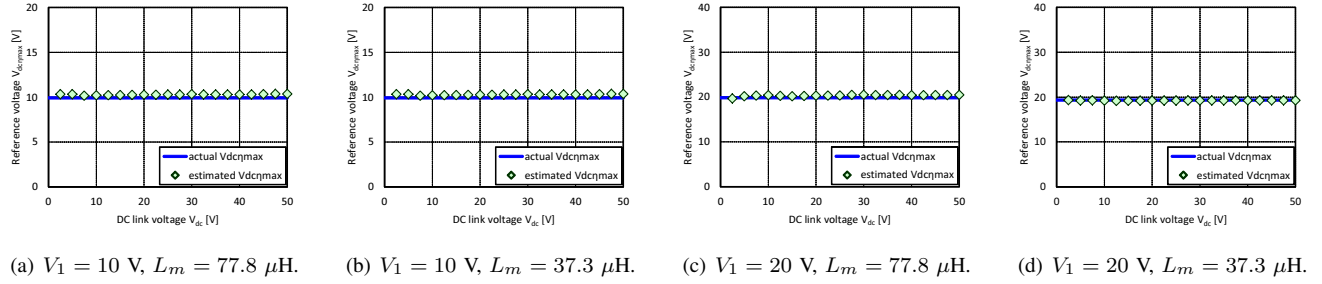


Fig. 10. Simulation results of reference voltage calculation for efficiency maximization.

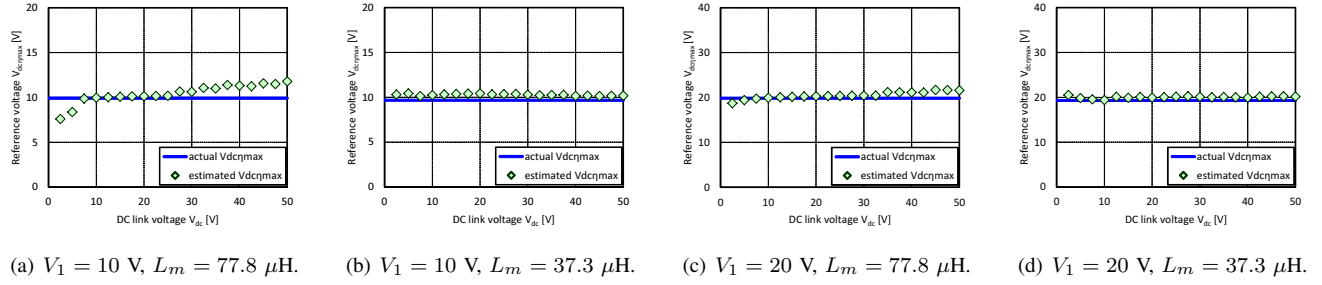


Fig. 11. Experimental results of reference voltage calculation for efficiency maximization.

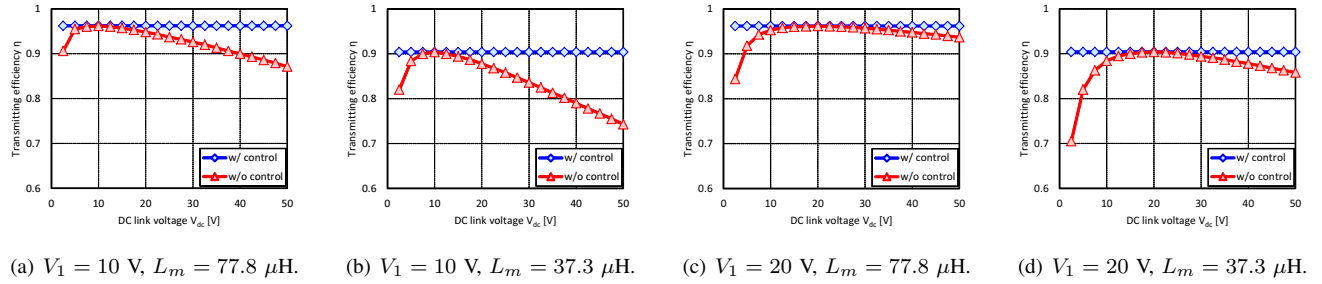


Fig. 12. Simulation results of efficiency maximization using calculated reference voltage.

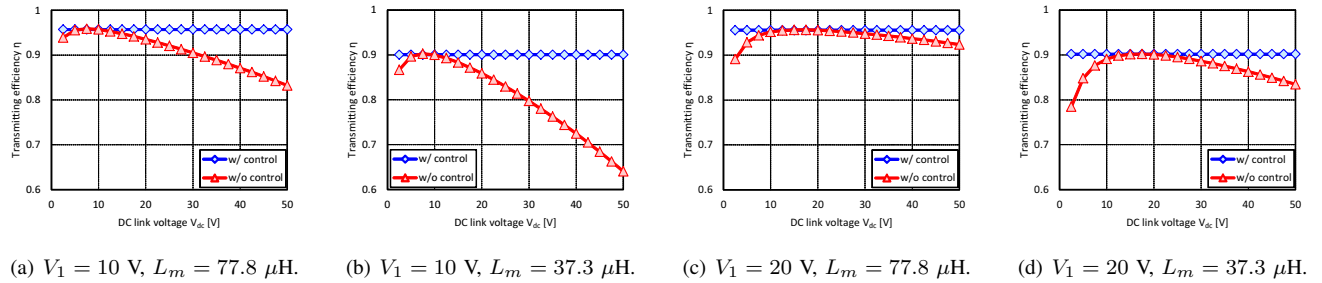


Fig. 13. Experimental results of efficiency maximization using calculated reference voltage.

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